ABSTRACT

Instance checking is considered a central tool for data retrieval from description logic (DL) ontologies. In this paper, we propose a revised most specific concept (MSC) method for DL SHI, which converts instance checking into subsumption problems. This revised method can generate small concepts that are specific enough to answer a given query, and allow reasoning to explore only a subset of the ABox data to achieve efficiency. Experiments show effectiveness of our proposed method in terms of concept size reduction and the improvement in reasoning efficiency.

Categories and Subject Descriptors
I.2 [Artificial Intelligence]: Knowledge Representation Formalisms and Methods

General Terms
Algorithms

Keywords
Data retrieval, Description Logic, Ontology, MSC, SHI

1. INTRODUCTION

One of the core tasks in Description Logic (DL) systems is to provide an efficient way to query the assertional knowledge (i.e. ABox $A$) in a DL ontology; and DL systems are expected to scale well with respect to (w.r.t.) the fast growing ABox data.

Instance checking that tests whether an individual is an instance of a given concept, is considered the most basic service for data retrieving from ontology ABoxes. A common intuition about realizing instance checking is the so-called most specific concept (MSC) method [1] that computes the MSC of a given individual and reduces instance checking of this individual into a subsumption test (i.e. test if one concept is more general than the other). More precisely, once the most specific concept $C$ of an individual $a$ is known, to check if $a$ is a member of any given concept $D$, it is sufficient to test if $C$ is subsumed by $D$ w.r.t. the terminological part (i.e. TBox $T$) of the ontology.

The computation of a MSC, however, could be difficult when qualified existential restrictions (i.e. $\exists R.C$) are supported by DLs. For example, when computing the MSC for individual $a$ given assertion $R(a, a)$, there may not exist a finite representation of the concept. Most importantly, the computation may involve assertions of other individuals that are connected to the given one through role assertions, which may consequently make the resulting MSC a large concept and reasoning with it degenerated into a prohibitively expensive procedure.

In this paper, we propose a revised MSC method that solves the above mentioned problems by using nominals [1] and applying a call-by-need strategy together with optimizations. The revised method takes into consideration only the related ABox information and computes a concept for each individual that is only specific enough to answer the current query w.r.t. the TBox. Based on this strategy, the revision allows the method to generate much simpler and smaller concepts than the original MSC’s by ignoring irrelevant ABox assertions. On the other hand, the complexity reduction comes with the price of re-computation for every new query if no optimization is applied. Nevertheless, as shown in our experimental evaluation, the achieved reduction could be significant in many practical ontologies, and the overhead is thus negligible comparing with the reasoning efficiency gained for instance checking. Moreover, due to the re-computations, the ABox data is amenable to frequent modifications, which is in contrast to the original MSC method where a relatively static ABox is assumed.

2. THE REVISED MSC METHOD

Without loss of generality, we assume every concept in a given ontology is in simple-form with maximum level of nested quantifiers less than 2. The original MSC of an individual $a$ preserves complete information of a w.r.t. the ABox $A$, denoted MSC($A, a$).

To apply the call-by-need strategy, we abandon this completeness and compute a concept that is only specific enough to determine if individual $a$ can be classified into current query concept $D$.

A simple way to realize this strategy is to assign a fresh name $A$ every time to a (complex) query concept $D$ by adding the axiom $A \equiv D$ to $T$, and to concentrate only on ABox assertions that would (probably) classify individual $a$ into $A$ w.r.t. $T$.

Theoretically, a sufficient and necessary condition for a role assertion $R(a, b)$ to derive individual classification $A(a)$ is that, the class term behind $A(a)$ be subsummed by concept $A$ w.r.t. $T$ [1]. More
precisely, this condition can be expressed as:

\[ \mathcal{T} \models \exists R.B \sqcap A_0 \subseteq A, \]  

(1)

where \( b \in B \), and concept \( A_0 \) summarizes other information that is also essential for this classification, with \( A_0 \not\subseteq A \).

As shown in [3], for (1) to hold when \( A \) is a named concept, there must exist some role restriction \( \exists R'.C \) with \( R \subseteq R' \) used in the TBox for concept definition; otherwise \( \exists R.B \) is not comparable (w.r.t. subsumption) with other named concepts (except \( \top \) and its equivalents). This syntactic premise is formally indicated by the following proposition.

**Proposition 2.1 ([3]).** Let \( \mathcal{K} = (\mathcal{T}, A) \) be a SHI ontology with simple-form concepts only, \( \exists R.B \) and \( A_0 \) be SHI concepts, and \( A \) a named concept. If

\[ \mathcal{K} \models \exists R.B \sqcap A_0 \subseteq A \]

with \( A_0 \not\subseteq A \), there must exist formulae in \( \mathcal{T} \) in the form as:

\[ \exists R'.C_1 \cong C_2 \sqsubseteq C_3 \]  

(2)

where \( R \subseteq R' \) and \( \triangleright \) is a place holder for \( \sqcup \text{ and } \sqcap \). Also note the following equivalence:

\[
\begin{align*}
\exists R.C \sqsubseteq D & \iff \neg D \sqsubseteq \forall R.\neg C \\
\exists R.C \sqsubseteq D & \iff C \sqsubseteq \forall R^-.D
\end{align*}
\]

This proposition is proven in [3]. It states in fact a syntactic premise in SHI for a role assertion to be essential for some individual classification. That is, if \( R(a, b) \) is essential for derivation of \( A(a) \), there must exist some related axiom in \( \mathcal{T} \) in the form of (2) for \( R \subseteq R' \). This condition can be further optimized by consider the following two cases for axiom (2):

1. if there is any concept \( B_0 \) in explicit class assertions of individual \( b \), such that \( \mathcal{K} \models B_0 \subseteq \neg C_1 \), or

2. if there is any concept \( A_0 \) in explicit class assertions of individual \( a \), such that \( \mathcal{K} \models A_0 \subseteq \neg(C_3 \sqcup \neg C_2) \) or \( \mathcal{K} \models A_0 \subseteq \neg C_3 \), respectively for \( \sqcap \) standing for \( \sqcap \) or \( \sqcup \).

Either one of the above cases happening, that particular axiom in fact makes no contribution to the derivation of \( A(a) \), unless the ABox is inconsistent where MSC’s are always \( \bot \). Thus, a revised condition requires not only the existence of related axiom (2) but also with none of the above cases happening. We denote this condition as \( \text{SYN}_\text{CDIN}\), and use it to rule out statements that are irrelevant to the current query. The computation of a specific-enough “MSC” (denoted MSC\(_\tau\)) should then only concentrate on assertions that are relevant. A recursive algorithm for this computation is given in the associated report.

### 3. EMPIRICAL EVALUATION

We implemented our method and tested it on a set of well-known ontologies with large ABoxes: benchmark ontologies LUBM (LM) and extended DBpedia (DP), and realistic biomedical ontologies AT and CE. More details of the evaluation can be found in the associated report.

To evaluate efficacy of the revised MSC method, we also implemented the original one for comparison. We compute the MSC\(_\tau\) for each individual in every ontology using the two methods respectively, and measure the complexity of the resulted concepts in terms of the maximum and the average depth of nested quantifiers (see Table 1). We report in Figure (1) the reasoning efficiency achieved when using the revised MSC method for instance checking, comparing with a complete ABox reasoning using DL reasoner HermiT [2], which implements various optimizations for the reasoning algorithm. We also compared our method with the modular reasoning reported in [3]. Efficiency in the initialization stage (e.g. ontology loading and reasoner initialization) can also be achieved using the MSC\(_\tau\) method, as it only needs to load a TBox while a compete reasoning requires loading of both the TBox and the big ABox.

### 4. CONCLUSION

In this paper, we proposed a revised MSC method for efficient instance checking. This method allows the ontology reasoning to explore only a much smaller subset of ABox data that is relevant to a given instance checking problem, thus being able to achieve great efficiency and to solve the limitation of current memory-based reasoning techniques. It can be particularly useful for answering object queries over those large non-Horn DL ontologies, where existing optimization techniques may fall short and answering object queries may demand thousands or even millions of instance checking tasks. Due to the independence between MSC\(_\tau\)’s, scalability for query answering over huge ontologies (e.g. semantic webs) can also be achieved by parallelizing the computations.

#### Table 1: Quantification depth of MSC\(_\tau\)’s

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#### Figure 1: Average time (ms) on instance checking.

### 5. REFERENCES

